
***Introduction to Integrated
Delay and Phase-Locked Loops
and Applications***

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- Introduction
 - Early 'history'
 - DLLs and PLLs what are they?
 - Making sure we understand each other
- Delay-Locked Loops
- DLL Applications
- Phase-Locked Loops
- PLL Applications

Early PLL History

- **1922 & 1927 First studies on oscillator synchronization:**
 - E. V. Appleton. “*Automatic synchronization of triode oscillators, part iii.*” Proc. Cambridge Phil. Soc., tome 21, pp. 231–248. 1922
 - B. van der Pol. “*Forced oscillators in a circuit with non-linear resistance. (reception with reactive triode).*” Phil. Mag., tome 3, pp. 64–80, 1927
- **1932 The first publication on the PLL concept:**
 - H. de Bellescise, “*La Réception Synchrone*”, Onde Electrique, vol 11, June 1932, pp. 230-240
- **1932 A team of British scientists develops the *homodyne (synchrodyne)* detection:**
 - The signal is mixed with that of a local oscillator having the same frequency as the carrier
 - The technique was devised to eliminate the tuned stages of the superheterodyne
 - The early name was Automatic Frequency Control
- **1943 The concept is applied in TV receivers to the synchronization of the vertical and horizontal scan (Wendt & Fredendall)**
- **1970 First integrated Phase-Locked Loops**
 - 1968 Hans Camenzind proposed the idea to Signetics
 - 1970 two Signetics products:
 - **Graham Rigby and Alan Grebene:**
 - Circuit based on an emitter-coupled oscillator
 - **Hans Camenzind:**
 - “The 565 came out three months later and is still being manufactured”
 - This development allowed the “explosion” of the applications of phase-locked loops
 - It is very likely that you have at least one in your pocket

What are DLLs and PLLs?

- For those of you that don't know the meaning of these two groups of three letters:
 - DLL → Delay-Locked Loop
 - PLL → Phase-Locked Loop
- Let's try to be more specific:
 - DLLs are negative feedback control systems that try to adjust the propagation delay of an internal circuit so that it matches the period of a reference signal.
 - PLLs are negative feedback control systems that try to adjust the oscillation frequency and phase of an internal oscillator so that they match the frequency and phase of a reference signal.
- These look like pointless operations!
 - The 'secret' is that:
 - DLLs track the 'average' period of the reference signal
 - PLLs track the 'average' phase (and frequency) of the reference signal
- We will spend some time trying to make these statements clear.

DLL/PLL = Control System

DLLs and PLLs are control systems:

- Intrinsically:
 - DLLs are first order systems
 - PLLs are second order systems
- In practice due to the chosen architecture or the practical implementation:
 - DLLs might become second order
 - PLLs might become third (or higher) order
- It is necessary to ensure that:
 - They are stable
 - The transient response is optimal
- Since PLLs and DLLs are control systems, standard control theory applies
- The quantity being controlled is not a position, velocity, temperature..., but:
 - The propagation delay in the case of a DLL
 - The oscillator phase and frequency in the case of a PLL

Linear / Non-linear?

- DLLs and PLLs are non-linear systems
- However, under certain conditions they can be considered linear and most of the theory is usually developed under that assumption
- We will look both at cases where a linear approximation can be used and cases where the systems have to be considered as non-linear

Why to study DLLs and PLLs?

- These circuits are becoming almost ubiquitous in electronic system:
 - From TV, passing through GSM, microprocessors... and down to memories
- The widespread use of these circuits is mainly due to monolithic integration:
 - Discrete implementations require a relatively high component count making them an expensive part of the system
 - Nowadays, due to the scale and integration potential of VLSI technologies these components are of modest complexity and represent only a small fraction of the system cost
- An engineer must thus be familiar with the basic concepts if he/she:
 - Wants to use it as a 'black box';
 - Needs to specify one;
 - Needs to design one for a specific application.

Applications

The range of applications is large. Here are some of the most important:

- Delay-Locked Loops:
 - Clock phase adjustment in clock domains of microprocessors
 - Sub-gate delay timing adjustment circuits
 - Multiple clock phase generators
 - Time-to-Digital (TDC) converters
- Phase-Locked Loops:
 - Jitter reduction
 - Skew suppression
 - Frequency synthesis
 - Clock recovery
 - Phase demodulation
 - Frequency demodulation
 - ...
- We will discuss in detail some of these applications

Frequency & Frequency!?

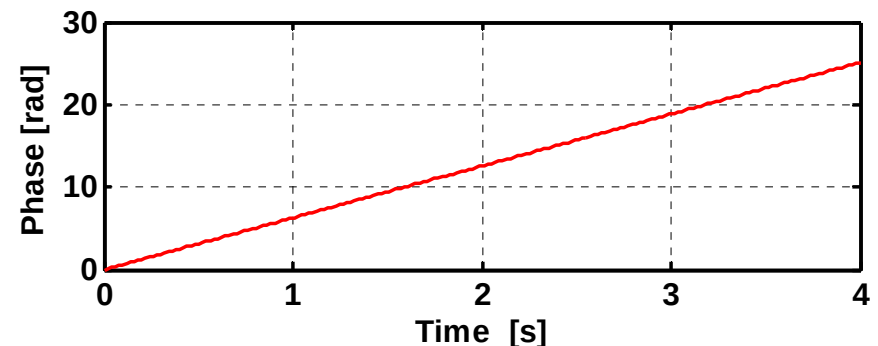
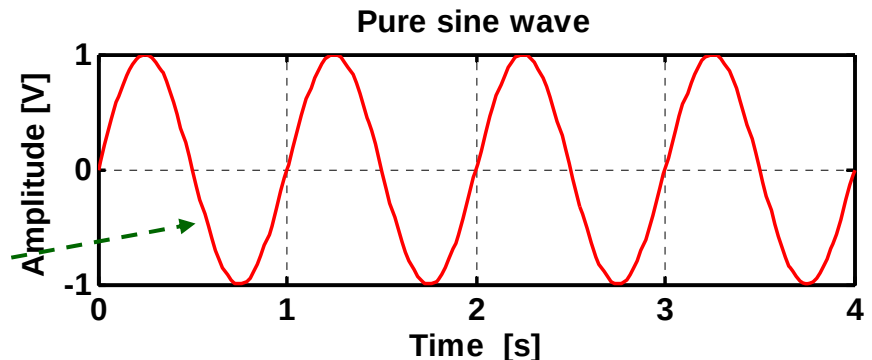
- Before proceeding it is important to clarify a point:
 - In the world of PLLs and DLLs, the word frequency is often used with respect to multiple concepts!
- Lets consider a signal that you know quite well: a pure sine wave:
 - The signal oscillates between two levels: $\pm A$
 - If we assume (for simplicity) its initial phase to be zero, the zero crossings are exactly at $t = n \cdot T$, with $n = \dots, -2, -1, 0, 1, 2, \dots$ and $T = 1/f_0$
- Mathematically this signal is written as:

$A \cdot \sin(2 \cdot \pi \cdot f_0 \cdot t + \phi_0)$

→
- To completely specify the signal, it is enough to specify:
 - Its amplitude: A
 - An initial phase ϕ_0
 - Its oscillation frequency: f_0

- We can, alternatively, describe the signal by its Fourier transform. This will lead to a frequency domain representation of the signal:
- Mathematically, two deltas of *Dirac* at $\pm f_0$ ($\pm \omega_0$) are used to represent the sine wave:

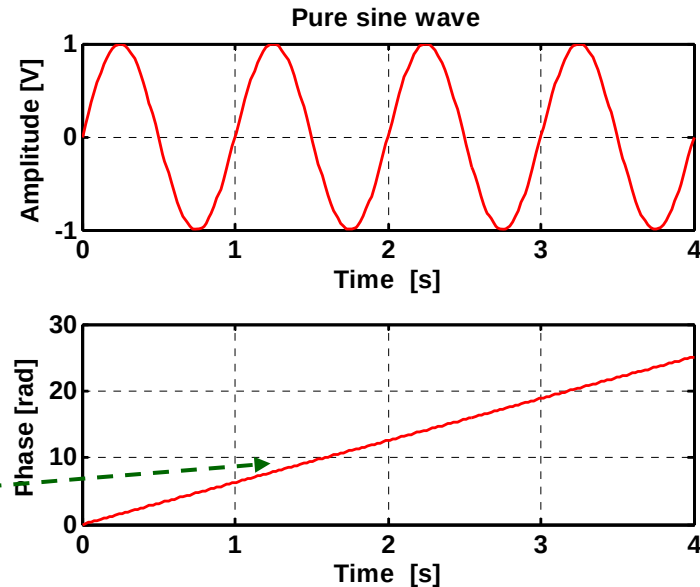
$A \cdot (j \cdot \pi \cdot \delta(\omega_0 + \omega) - j \cdot \pi \cdot \delta(\omega_0 - \omega))$



Phase is most important

- DLLs and PLLs are devices sensitive to the phase:
 - They are “insensitive” to the amplitude of the signal (almost always)
- Thus, to analyze a DLL or a PLL it is enough to know how the signal phase behaves as function of time (or, in more ‘fancy words’, in the time domain):

$$2 \cdot \pi \cdot f_0 \cdot t + \phi_0$$



- In the case of the ‘pure’ sine wave (starting at time $t=0$), the phase is a ramp of slope: $2 \cdot \pi \cdot f_0$
- Alternatively, we can take a Fourier transform of the phase signal and obtain its frequency domain representation:

Time domain

$$\phi(t) = 2\pi \cdot f_0 \cdot \int u(t) dt$$

Frequency domain

$$\phi(f) = \frac{f_0}{j \cdot f} \cdot \left[\frac{1}{j \cdot 2\pi \cdot f} + \frac{1}{2} \delta(f) \right]$$

A more realistic phase signal

Example:

Noisy square wave oscillator.

- Mathematically:

$$s(t) = \text{sign}[\sin(\phi_s(t))]$$

where:

$$\phi_s(t) = 2 \cdot \pi \cdot \langle f_o \rangle \cdot t + \phi_0 + \int_{-\infty}^t f_n(t) dt$$

The signal is strictly not periodic but it is still possible to define an average frequency

The frequency noise is a random variable with zero mean

The phase noise is cumulative, that is, the 'end' of a cycle is the 'starting point' of the next.

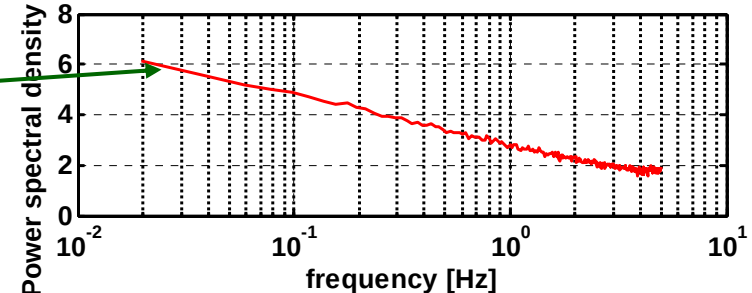
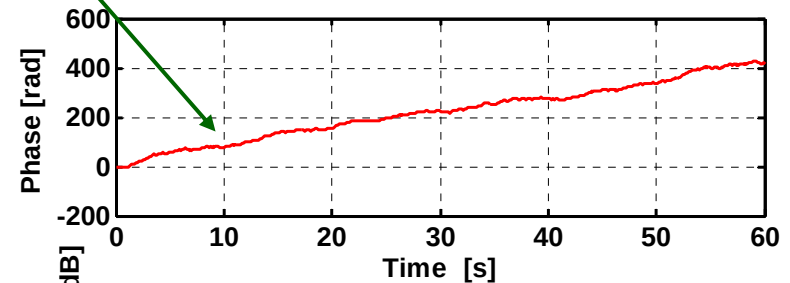
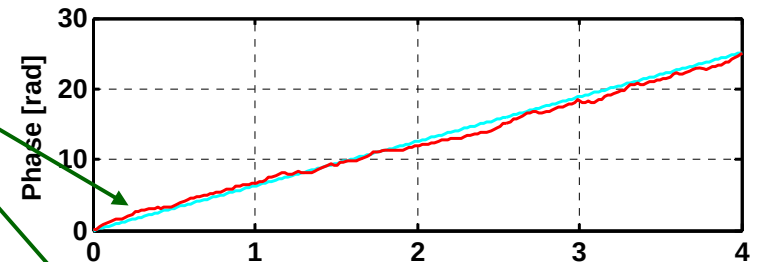
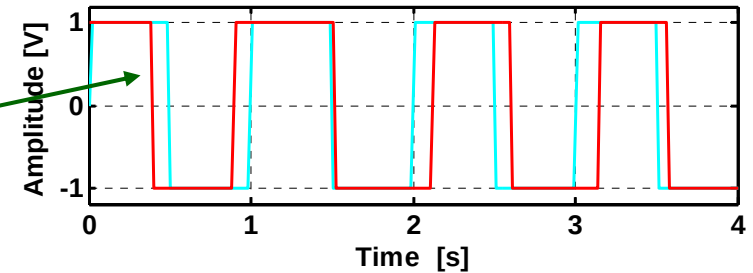
The phase noise is also called jitter

- For each outcome we can define the Fourier transform $\phi_s(f)$, but in this case the meaningful quantity is the power spectral density:

$$\phi_{ss}(f) = \lim_{T \rightarrow \infty} \frac{\langle \phi_s(f) \cdot \phi_s^*(f) \rangle}{2 \cdot T}$$

This is the quantity you can measure using a spectrum analyzer

Noisy square wave



Summarizing

We are “only” interested in the Phase

- PLLs and DLLs lock to “periodic” signals;
- In general these signals have both time dependent amplitude and phase;
- PLLs and DLLs are sensitive to the signal’s phase (and not amplitude);
- Since the phase is **the** signal we can look at it both in:
 - The time domain;
 - The frequency domain.
- The phase signal has both:
 - A time domain representation $\phi(t)$
 - A frequency domain representation $\phi(f)$, $\phi(\omega)$ or Laplace transform $\phi(s)$
- Example: consider a PLL locked to a 1 GHz jittery clock signal:
 - The average frequency of the reference signal is 1 GHz;
 - Its VCO is working at an average frequency of 1 GHz;
 - This PLL might have, e. g., a 10 MHz signal bandwidth only;
 - This means that any spectral content of the phase noise that is above 10 MHz will be low-pass filtered by the PLL phase transfer function.